# SPAN OF CONTROL: A COMPARATIVE FACTOR ANALYTIC APPROACH\*

by Emmanuel T. Velasco

### INTRODUCTION

How many subordinates can a manager effectively supervise?

The ratio of subordinates to superior is defined as the span of control or management. Urwick normatively fixed the chief executive's span at four and the front-line supervisors to between eight and twelve. In practice, widely varying span can be found among different companies suggesting that there are many factors to consider in deciding the appropriate span.

Those who have written on the topic of span of control primarily specify a few of its various determinants and, in some instances, attempt to verify the nature of the relationship between these independent variables and the span of control. However, except in the case of Meyer<sup>2</sup>, no other writer has attempted to integrate the various determinants and present a unified set of hypotheses about the relationship between the relevant variables. For sure, this will be the direction of future research work.

The author's objective in this paper is to collect the various determinants of the span of control that have been mentioned in the literature and attempt to establish the factors which involve the most paralmonious description of the dimensions of the span of control using the statistical technique of factor analysis.

The author wishes to acknowledge the University of Chicago and University of the Philippines Computer Centers for the computations.

Urwick, "The Manager's Span of Control," Harvard Business Review 34 (May, 1956) pp. 39-47.

Meyer, "A Theory of Departmental Structure of the Formal Organizalin," Unpublished Ph.D. dissertation, Graduate School of Business, University of Chicago, 1967.

The next section is a description of the steps that Lockhead Missile and Space Company undertook in constructing an index of supervisory burden and how this index was used in predicting the appropriate span of control. Section 3 is a discussion of other span factors that have been mentioned in the literature. Section 4 considers the results of the factor analysis based on the responses of American and Filipino subjects.<sup>3</sup> Section 5 is the concluding section.

## INDEX OF SUPERVISORY BURDEN

Stieglitz [8] gives an account of how Lockhead Missile and Space Company developed an index of supervisory burden. First, the company officials defined the span factors they found to have caused differences in the span of control in various sections of their plants; namely:

- (1) Similarity of functions (similarity of the activities performed by the subordinates);
  - (2) Geographical contiguity (disperson of the subordinates);
  - (3) Complexity of functions (nature of the tasks done);
  - (4) Direction and Control (nature of the subordinates; the amount of training and attention needed by them);
  - (5) Coordination (time needed to coordinate the activities of various units); and
  - (6) Planning (the scope and complexity of activities to be planned).

The next step was to establish a point system to determine the degree of supervisory burden of each of these span factors. A five point scale was used, ranging from 1 to 5, for similarity of functions and geographical contiguity; 2 to 10 for complexity of functions, coordination, and planning; and 3 to 15 for direction and control. Thus, the point system applied also determined the relative weights given to each of the factors.

<sup>&</sup>lt;sup>3</sup>The results based on the responses of the American subjects were first presented in a term paper submitted by the author while he was a doctoral student at the University of Chicago, to Prof. John Humpal as part of the requirements of the course, Business 360 (Organization: Structure and Process).

The sum of the points given for each of these factors in evaluating a particular position in the firm constituted a raw index which was then corrected for the amount of organizational assistance received by the superior. Informally, weight was also given to the competence of the individual superior in the computation of the final index.

Using this index of supervisory burden, various units of the firm were rated and a regression analysis was done between the computed index and the actual span of control. It is interesting to note that a significantly different relationship was established for front-line supervisors and middle managers.

The attempt of Lockhead to make the concept of optimizing the span of control operational in terms of an index of supervisory burden is bound to find application in other firms. However, there may be other span factors that have not been considered important by Lockhead's management that cause differences in the span of control for other firms.

The next section surveys the literature in terms of other span factors that have been found to cause differences in the span of control.

### OTHER SPAN FACTORS

Terrien and Mills<sup>4</sup> found that increasing organization size, as measured by total employment, is associated with a decline in the span of control. Fisch<sup>5</sup>, however, found a tendency for the span of management to be smaller as the company size decreased. Anderson and Warkov<sup>6</sup> found a larger span in large organization and a smaller span in organization with a wide product range which led them to make a hypothesis that perhaps differences in product range and geographical dispersions of the firms included in their sample obscured the real relationship between the size and span of control.

<sup>&</sup>lt;sup>4</sup> F. Terrien and D. Mills, "The Effects of Changing Size Upon the Internal Structure of Organization," American Sociological Review 20 (February, 1955), pp. 11-13.

<sup>&</sup>lt;sup>5</sup>G. Fisch, "Stretching the Span of Management," American Sociological Review, 61 (Sept./Oct. 1963), pp. 74-85.

<sup>&</sup>lt;sup>6</sup> T. Anderson and S. Warkov, "Organization Size and Functional Complexity," American Sociological Review, 26 (February 1961), pp. 24-28.

Perhaps another intervening variable is technology. Woodward<sup>7</sup>, afte classifying firms in her sample into three groups in terms o production methods used, found that within each group the span o control of the chief executive increased directly with the level o technical complexity of the production methods, and the span of the front-line supervisors increased from unit to mass production bu subsequently declined with process production.

Woodward also found an increase in the number of professional employed by the firm as the level of technical complexity increased. Thus, the degree of professionalism may be another factor that affects the span of control in terms perhaps of ease of communication.

Whisler et. al. stated that "control can be assigned in a variety of alternative pattern at the discretion of leadership, with technology organization size and other factors... The pattern of control that it established determines a homologous pattern of role demands... These role demands can be expressed in terms of individual attributes: innate intelligence, acquired special or general knowledge energy, sensitivity, insight and daring..." Thus, individual attributes of the subordinates may be considered as another variable affecting the span of control.

Jacques<sup>9</sup> considered the amount of discretionary aspect of the job as the relevant measure of the size of the job of the subordinate and thus, the variable subject to the control by the superior. Moreover, the review mechanism used by the superior, i.e., direct vs. indirect, also determines the number of subordinates he can effectively supervise.

Hill<sup>10</sup>, in applying queuing theory to the span of control, assigned numerical values to such variables as the length of an average session of the subordinate with his superior, the average interval between

<sup>&</sup>lt;sup>7</sup>J. Woodward, Management and Technology (London: HMSO, 1958).

<sup>&</sup>lt;sup>8</sup>T. Whisler, et. al. "Centralization or Organizational Control," Journal of Business, 50(January, 1967), pp. 10-26.

<sup>&</sup>lt;sup>9</sup>E. Jacques, The Measurement of Responsibility (Cambridge: Harvard University Press, 1956).

<sup>&</sup>lt;sup>10</sup>L. Hill, "Application of Queing Theory to the Span of Control," Academy of Management Journal, 6(March 1963), pp. 58-69.

mension, the cost of subordinates' and superiors' time, and the cost incurred with delays in having sessions with superior. Perhaps all these factors can be subsumed into the cost of queuing time.

Koontz and O'Donnell<sup>1</sup> preferred to explain differences in span of control in terms of factors that affect the frequency and severity of superior-subordinate relationships. They mentioned the following:

- (1) The relative difficulty of training subordinates;
- (2) Adequacy and clarity of authority delegation;
- (3) Planning (workable plans and plans consistent with goal);
- (4) Rate of change in objectives, policies and production process;
- (5) Use of objective standard in evaluating subordinate's performance;
- (6) Communication techniques used by superior and subordinates;
- (7) Amount of personal contact required of superior (e.g., conferences and committee meetings); and
- (8) Functional authority imposed on superior (e.g., personal matters handled by front-line supervisors).

In discussing how decentralization improved the efficiency of Bears Roebuck and Company, Worthy<sup>12</sup> brought out the relationship between span of control and the number of organization levels.

Finally, Meyer<sup>13</sup> first looked into various communication impediments and then later presented hypotheses relating them to the apan of control. He classified communication impediments into these categories:

HIII, 1968), pp. 247-51.

J. Worthy, "Organization Structure and Employee Morale," American Moclological Review 15(April 1960), pp. 169-179.

Meyer, op cit.

- (1) Nature of the employees;
- (2) Nature of the communication media used;
- (3) Geographical distance and other physical impediments;
- (4) Nature of the jobs controlled;
- (5) Communication interferences: volume of vertical communication; and
- (6) Communication interferences: number of organization levels.

In Meyer's theory, the span of control is largely determined by the trade-off between two opposing factors — costs of superior-exerted control and the economies from superior-exerted control. The hypotheses he presents are:

- (1) The higher the economies from superior-exerted control, the smaller the span of control;
- (2) The more the firm uses substitutes for control (manuals, rules and regulations), the less it uses superiors and thus, the larger the span of control;
- (3) The span of control tends to be larger in firms where the impediments exist to a larger degree (because firms tend to reduce the costs of superior-exerted control by selecting better employees and using written communication);
- (4) The higher the interdependency of a firm's jobs, the narrower the span of control;
- (5) The more extensive the use of Electronic Data Processing (EDP) by a firm, the smaller its span of control;
- (6) The more expansive the vertical communication, the larger the span of control; and
- (7) Certain qualities in employees such as intelligence, job skills, personality traits (including motivation), facilitate the ease with which an employee is able to control or be controlled.

# The Questionnaire

A questionnaire was constructed on the basis of the various determinants of span of control that were discussed above. (Appendix A). The questionnaire includes thirty variables each of which had to be rated on a 5-point important-not important scale.

The basic assumption in a study of this type is that the respondents are adequately exposed to formal organizations such that they can discern factors causing differences in the span of control. Ideally, the respondents should come from a firm or an industry so that the results can be validated with the actual situation. As usual, however, the questionnaires were administered to students. The results, therefore, should be taken as tentative and conditional in nature.

Two sample groups were considered. The American respondents were from the Graduate School of Business of the University of Chicago who, at the time they filled up the questionnaire, were enrolled in the course: ORGANIZATION STRUCTURE AND PROCESS. A total of 35 completed questionnaires were collected from this group. Subsequently, a matching group of 35 Filipino respondents who were students in BUSINESS POLICY I at the MBA program of the University of the Philippines were selected to fill up the questionnaire.

The span variable complexity of activities performed by subordinates garnered the highest mean rating of 4.31 (i.e., most important) among the Filipino respondents while the variable personality characteristics and capability of the manager was listed most important (mean = 4.00) by the American respondents. The Filipino respondents considered use of Electronic Data Processing (EDP) by the firm least important (mean = 2.54) while the American respondents rated the number of products as the least important variable (mean = 1.54). The standard deviation of these variables are 10, 1.01, 1.10, and .65, respectively.

The responses of each group were factor analyzed separately to determine their perceived dimensions of the span of control. Then the factors of these two groups were compared using the coefficient of congruence.<sup>14</sup>

<sup>&</sup>lt;sup>14</sup>H. Harman, Modern Factor Analysis: (Chicago: University of Chicago Press, 1967), p. 270.

### THE RESULTS

The computer program generated the factor loadings for thirt variables using the Principal Component Method. The resultin factors were then rotated by the use of the Varimax Method<sup>15</sup> to arrive at an orthogonal multiple factor solution.

The following tables present the ten factors that came out of the factor analysis of the responses of the Filipino subjects and the twelve factors that were extracted from the responses of the American subjects. Only those variables with loading greater or equato an absolute value of .4 were included in a factor. Moreover whenever a variable appeared in two or more factors, it was assigned only to the factor which carried the higher loading.

The ten factors extracted for the Filipino respondents explain 70.91 per cent of the total variance while the twelve factors for the American respondents explain 82.86 per cent of the total variance.<sup>16</sup>

The interpretation of these span factors is more or less straight forward. Some illustrations are:

### (1) Factor FI.

The more objective the standards applied in assessing a subordinate's performance and the more formal the review mechanism used by a superior in evaluating the performance of his subordinates, the wider is the span of control. This factor can perhaps be labelled as the nature of performance evaluation.

# (2) Factor A2:

The less the time in which the needed effort is exerted to coordinate the activities of subordinates, the smaller the amount of the discretionary content of a manager's job, and the smaller the volume of vertical communication in the organization, the wider is the span of control. This factor may be labelled as aspects of coordination.

<sup>15</sup> Ibid

<sup>&</sup>lt;sup>16</sup>The sum of the squared given values for the two groups are 23.7418 and 24.8570. These figures are divided by the no. of variable (=30) to arrive at the proportion of the total variance explained by the factors extracted.

# (8) Factor F2:

The more interdependent the jobs are, the more motivated the subordinates (i.e., motivation as an overall measure of their personality attributes) are; and the more organization assistance is provided to the superior, the wider is the span of control. The nature of jobs and people may be a label that we can attach to this factor.

### Table 1.1

# Dimensions of the Span of Control Filipino Subjects (N = 35)

ADIADIEC

LOADINGS

ľ	ACTO	ORS VARIABLES DONE	11100
	F1	Objectivity of standards applied in assessing	00
		subordinate's performance	.82
		Review mechanism used by superior in evaluating	
		subordinate's performance	.76
	TO O	Degree of job interdependence	.80
	F2	Personality attributes of the subordinates	.60
		Amount of organizational assistance received by	
		the superior	.55
		the superior	
	ma	Adequacy and clarity of authority delegated to the	
	F3	superior	84
		Degree of professionalism of employees	81
		Personal characteristics of manager	
		Number of organizational levels	45 74 76
		Number of organizational levels	
		Functional authority imposed on superior	.88
	F4	Amount of training of the subordinates	
		Amount of training of the subordinates	
	TO #	Size of the organization	.87
	F5	Nature of the production processes used by the	
		firm	71
	1	Volume of vertical communication	
	F6	The rate of organizational change	.72
		The rate of organizational change	1000
		Volume of horizontal communication	100
		Nature of the communication media used	
		Scope and complexity of activities to be planned	83
	107	Scope and complexity of activities to be plained	

го	Cost of subordinate's queing time to the superiors Availability of manuals, rules and regulations as substitute for superior exerted control	
F9	Job skills possessed by subordinates Similarity of activities performed by subordinates Complexity of activities performed by subordinates	1Z
F10	Number of products	.45 53
	Table 1.2	-
	Dimensions of the Span of Control American Subjects (N = 35)	
FACTOI	RS VARIABLES LOAD	INGS
A1	Number of products	.81 .68 .68
A2	Time and effort needed to coordinate subordinates' activities	70 64 54
A3	Personality attributes of the subordinates Cost of subordinate's queuing time to see superior	73 58 58
A4	Complexity of activities performed by subordinates . Personality characteristics and capability of manager .	.74 40

Time and effort needed to coordinate subordinate's

Discretionary contents of manager's job . . . . . . .

Amount of personal contacts required of manager . . .

A5 Nature of the communication media used .....

AR	Amount of training of subordinates	.76
AU	Job skills possessed by subordinates	.75
	The rate of organizational change	.44
A7	Geographical dispersion of subordinates	76
	Discretionary content of subordinates' job	74
	Degree of job interdependence	53
A8	Volume of congenial communication	+.51
AO	superior	78
	Degree of professionalism of employees	58
	Adequacy and clarity of authority delegated to	X/
	the subordinates	41
A9	Availability of manuals, rules and regulation as	
	substitute for superior exerted control	.81
	Similarity of activities performed by subordinates	.50
A10	Functional authority imposed on supervisor	.86
A11	The nature of the production process used by the	1000
	firm	86
A12	Review mechanism used by superior in evaluating a	
	subordinate's performance	86
	Objectivity of standard applied in assessing a	54
	subordinate's performance	04

One can proceed to interpret and attach labels to the other factors noting the signs of the factor loadings of the variables. In so doing, some of the factors will appear to include variables that do not go together. Thus,

# (1) Factor F3:

The less professionalism and the less adequate and clear authority delegation existing in the organization should bring about a shorter span and not a longer span, just as fewer number of organizational levels (i.e., a flat organization) and the presence of more capable managers should lead to wider spans. In other words, there appears to be inconsistency in the sign of two out of the four variables included in this factor.

# (2) Factor F9:

The less job skills possessed by subordinates and the less complex the activities performed, the wider is the span but the sign of these two variables does not seem to go with the sign of the variable similarity of activities. It is expected that the more similar the activities performed by the subordinates, the wider is the span of control.

# (3) Factor A4:

When the activities performed by subordinates are more complex, the result should be shorter spans and not longer ones. On the other hand, the more competent the manager is, the wider (not narrower) should be the span.

# (4) Factor A7:

The less dispersed geographically are the employees and less the discretionary content of the job, the wider is the span of control; but less interdependent jobs and a large volume of horizontal communication should require a shorter and not a wider span of control.

In comparing the Filipino span factors with the American span factors, F1 and A12 stand out but are in direct conflict. While the two factors include the same variables, the factor loadings of these variables are opposite in sign. Thus, there is a positive relationship in F1 but a negative relationship of the variables objectivity of standards and formality of the review mechanism used in the evaluation of performance in A12.

One can also note from Table 1.1 and 1.2 that variables included in the Filipino factor are not always the same variables included in an American factor. In other words, while some overlaps exist between Filipino and American factors, the variables do not always match. A test of the similarity of factors extracted from two different groups using a fixed set of variable is the coefficient of congruence. Table 2 gives the coefficient of congruence that are equal or greater than 0.4 in absolute values for the factors of the two groups with overlapping variables.

Positive coefficients in Table 2 indicate similarity of Filipino-American factors while the negative ones show dissimilarity of Filipino-American factors. There are only four sets of factors which can be considered as fairly similar dimensions of the span of control

there hand, there are eight combinations of Filipino-American factors which turned out to be fairly dissimilar. In general, therefore, the can conclude that the perception of Filipino and American factors students in business differ as to the importance of variables affecting the span of control. This may be due to a number of factors of their than cultural differences such as exposure to formal organizations, age, etc. which cannot be held constant.

It is also possible that a questionnaire effect exists. Although the variables included in the questionnaire administered to the Filipino respondents were the same as those in the questionnaire administered to the American respondents, the arrangement of these variables was deliberately altered. This was an attempt to test the stability of the responses. Based on the results, it seems that the variation in the design of a research instrument may bring about different responses were among the same respondents.

#### CONCLUSION

The results of this study show that Filipino and American maduate business students perceive different factors affecting the partial differences, the perception of span of control factors may be studied in the affecting an appropriate span of control as summarized in the questionnaire used in this study may be a convenient starting that in the development of a Lockhead-type of an index of supervisory burden.

In a specific application to a firm, a factor analysis approach may be pursued to reduce these variables to a meaningful few. Assuming that the dimensions extracted from the factor analysis are appropriate, then one can proceed to the construction of an operational index of factors. However, instead of a subjective weighing scheme inhodied in the Lockhead method, one may use the average of the mean response of the variables included in each of the factors divided by the total of these averages as weights. In other words, suppose there are  $i=1,\ldots,n$  responses for each factor:  $A(i)=\sum_{j=1}^M \overline{X}(ij)$  where X(ij) is the mean response on the jth variable of the ith factor. Then the weights applied to these factors can be objectively determined as

$$W(i) = A(i)/\sum_{i=1}^{n} A(i)$$

 $i=1,\ldots,n$ 

The index  $I = \sum_{i=1}^{n} 100 \text{ W(i)(Fi)}$  where F(i) is the ith factor score can then be correlated with the actual span of control to establish its validity.

Table 2

Comparison of Filipino and American Span of Control Factors Using the Coefficient of Congruence

Similar Factors:	Coefficient o Congruence			
F4 and A10	0.59			
F5 and A1	0.51			
F10 and A1	0.47			
F8 and A7	0.40			
Dissimilar Factors:				
F5 and A11	-0.61			
F2 and A8	-0.55			
F1 and A12	-0.52			
F9 and A4	-0.52			
F6 and A5	-0.48			
F7 and A2	-0.47			
F9 and A6	-0.46			
F3 and A8	-0.45			

Alternatively, one can proceed to directly estimate the relationship between the span of control and the dimension of the span of mentrol extracted from the factor analysis using regression analysis. Here, the actual span of control found in the firm under study will be treated as the dependent variable while the span factors will be the independent variables. The derived equation will then provide an independent check of the sign of the span factor extracted from the factor analysis.

### BIBLIOGRAPHY

- Anderson, T. and Warkov, S. "Organization Size and Functional Complexity," American Sociological Review, 26 (February 1961), 24-28.
- Fisch, G. "Stretching the Span of Management," Harvard Business Review, 61 (September/October 1963), 74-85.
- Harman, H. Modern Factor Analysis, Second Edition Revised. Chicago: University of Chicago Press, 1967.
- Hill, L. "Application of Queuing Theory to the Span of Control," Academy of Management Journal, 6(March 1963), 58-69.
- Jaques, E. The Measurement of Responsibility. Cambridge, Massachusetts: Harvard University Press, 1956.
- Koontz, H. and O'Donnell, C. Principles of Management. New York McGraw Hill, 1968, 247-51.
- Meyer, H. "A Theory of Departmental Structure of the Forma Organization," Unpublished Ph.D. dissertation, Graduate School of Business, University of Chicago, 1967.
- Stieglitz, H. "Optimizing the Span of Control," Management Record, 24 (September 1962), 25-29.
- Terrien, F. and Mills, D. "The Effects of Changing Size Upon the Internal Structure of Organizations," American Sociological Review, 20 (February 1955), 11-13.
- Urwick, L. "The Manager's Span of Control," Harvard Busines Review, 34(May 1956), 39-47.
- Whisler, T. et. al. "Centralization or Organizational Control," Journa of Business, 50(January 1967), 10-26.
- Woodward, J. Management and Technology, London, HMSO, 1958
- Worthy, J. "Organization Structure and Employee Morale," American Sociological Review, 15(April 1950), 169-179.

## APPENDIX A

# QUESTIONNAIRE ON THE SPAN OF CONTROL

The following have been mentioned in the literature as possible determinants of the span of control — the ratio of the number of subordinates to a superior. Please go over the list first and then rate the importance of these determinants using the following five point scale:

- 1 not important
- 2 slightly important
- 3 important
- 4 moderately important
- 5 very important

# PLEASE ENCIRCLE THE APPROPRIATE NUMBER

		Not important		Very important			
1	Complexity of activities performed by subordinates	1	2	3	4	5	
9	Job skills possessed by subordinates	1	2	3	4	5	
8	Geographical dispersion of subordinates	1	2	3	4	5	
4	Similarity of activities performed by subordinates	1	2	3	4	5	
Đ,	Amount of training of the subordinates	. 1	2	3	4	5	
6.	Discretionary content of subordinate's job	1	2	3	4	5	
7	Degree of professionalism of employees	1	2	3	4	5	
8.	Adequacy and clarity of authority delegated to the subordinates	1	2	3	4	5	
9.	Personality attributes of the subordinate	es 1	2	3	4	5	
10.	Nize of the organization	1	2	3	4	5	

11. Nature of the production process used		2	3	4
by the firm	1	Z	0	4
12. Number of products	1	2	3	4
13. Use of EDP by the firm	1	2	3	4
14. Number of organizational levels	1	2	3	4
15. Scope and complexity of activities to be planned	1	2	3	4
16. Cost of subordinate's queuing time to see superiors	1	2	3	4
17. The rate of organizational change	1	2 .	3	4
18. Volume of vertical communication	1	2	3	4
19. Volume of horizontal communication	1	2	3	4
20. Nature of the communication media used	1	2	3	4
21. Degree of job interpendency	1	2	3	4
22. Functional authority imposed on superior	1	2	3	4
23. Amount of organizational assistance received by the superior	1	2	3	4
24. Availability of manuals, rules and regulations as substitute for superior-exerted control	1	2	3	4
25. Discretionary content of manager's job	1	2	3	4
26. Amount of personal contacts required of manager	1	2	3	4
27. Time and effort needed to coordinate subordinates' activities	1	2	3	4

98.	Objectivity of standard applied in assessing a subordinate's performance	1	2	3	4	5
99.	Review mechanism used by superior in evaluating a subordinate's					
	performance	1	2	3	4	5
80.	Personal characteristics and					
	capability of manager	. 1	2	3	4	5