FOR CASH: A PEDAGOGICAL NOTE

By

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It seems likely that the papers by Burnol and Tobin dealing with me relationship between the interest rate and the transactions semand for cash are on most reading lists for courses in macro mory and monetary economics. Students have probably puzzled wer the objective function used by Baumol in his model, in view of Tubin's remark that "Baumol's calculation of interest cost is rather mifficult to understand" on the ground that Baumol makes interest proportional to the average cash balance. This would seem to mply, according to Tobin, that interest cost would be zero in the mustion where cash is withdrawn from investment only at the moment when it is needed, but this would entail infinitely high brokerage costs, so that "it hardly seems a logical zero from which to measure interest costs." Tobin's own formulation of the problem is maximize interest earnings net of brokerage costs. Interestingly mough, though not really surprisingly, the use of Tobin's objective function in Baumol's framework gives the same formula as Baumol's.

Following Baumol, let T be the amount of dollars which is to be add out uniformly over a unit period of time; b + kC the broker's when C dollars are withdrawn from investment; and i the rate of the test. The number of withdrawals is n = T/C and, following Tobin, wish to choose C so as to maximize interest earnings net of total toker's fees (b + kC)n. Figure 1 depicts the situation.

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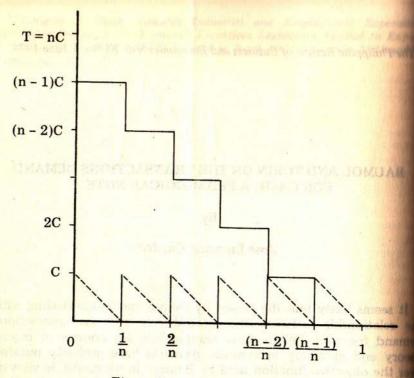


Figure 1

Each withdrawal C suffices to finance pay-out requirements for 1/2 of the period. During the first interval, the invested funds (n-1) earn interest equal to (n-1)Ci/n; during the second interval, interest earnings amount to (n-2)Ci/n, etc. Total revenue R thus amount to

$$R = (n-1)Ci/n + (n-2)Ci/n + ... + 2Ci/n + Ci/n$$

$$= (n-1)Ci/2 = (T-C)i/2$$

Net revenue NR is therefore NR = (T - C)i/2 - (b + kC)T/C and maximizing this with respect to C gives Baumol's formula

$$C = (2bT/i)^{1/2}$$

We see that since the interest earned is (T-C)i/2, the average amount invested must be (T-C)/2. This fact could have been obtained directly from observing that, because of the uniform page

the average balance (including funds invested and the cash balance) is T/2 while the average cash balance is C/2.

In Baumol's formulation of the problem, the objective was to

$$(b + kC)T/C + Ci/2$$

where Ci/2 is what Baumol calls the interest cost of holding cash. It is hear why we get the same formula as Baumol's, as minimizing this appression is equivalent to maximizing NR since Ti/2 is a constant.

REFERENCES

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